

NAME: \_\_\_\_\_

Student Number: \_\_\_\_\_

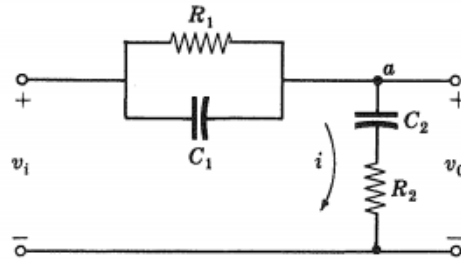
**Question 1**

Expand the equation below in the form of partial fractions.

$$Y(s) = -\frac{[s^2 + s - 10]}{s^3 + 3s^2 + 2s}$$

**Question 2**

Find the transfer function of the lead-lag compensator shown in Fig. Q2 below.



**Question 3**

Use block diagram reduction technique, find the transfer function  $C(s) / R(s)$  of the block diagram shown in Fig. Q3.

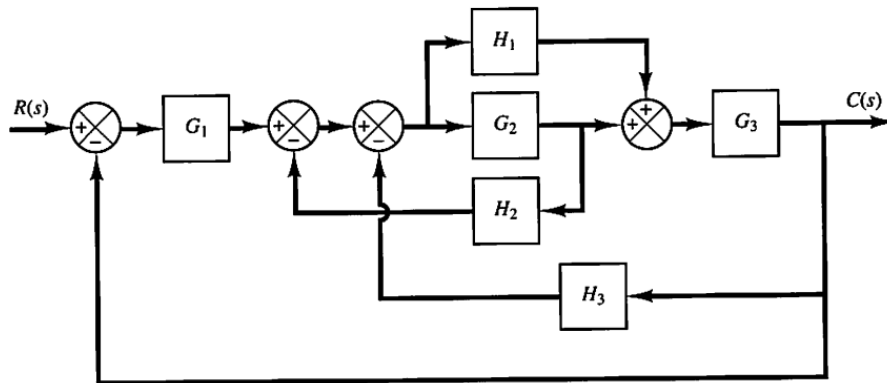


Fig. Q3

**Question 4**

For the Signal Flow Graph shown in Fig. Q4, find: (a) the input node(s); (b) the output node(s); (c) the path-gain of the forward path(s); and (d) the loop gains of the feedback loop(s).

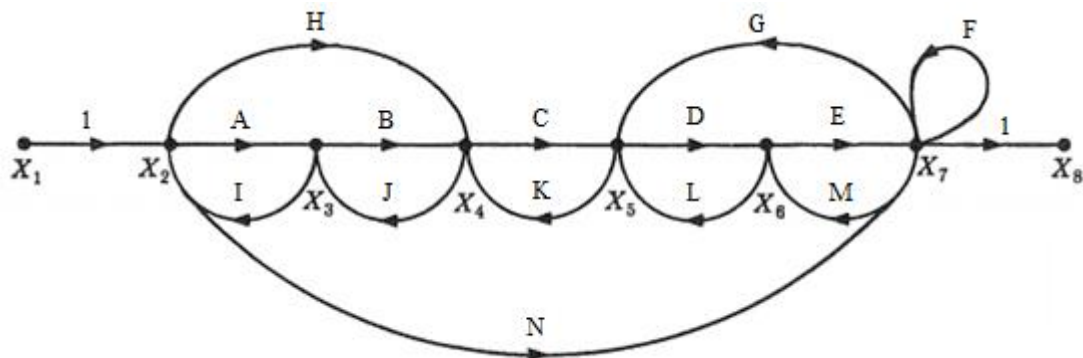


Fig. Q4

## QUESTION 1

$Y(s)$  can be written as follow,

$$Y(s) = \frac{-[s^2 + s - (10)]}{s(s+1)(s+2)} = \frac{A}{s} + \frac{B}{s+1} + \frac{C}{s+2}$$

Equating the numerator, we have

$$A(s+1)(s+2) + Bs(s+2) + Cs(s+1) = -[s^2 + s - (10)]$$

$$\text{if } s = 0, \quad A = \frac{10}{2}$$

$$\text{if } s = -1, \quad B = -(10)$$

$$\text{if } s = -2, \quad C = \frac{8}{2}$$

$$Y(s) = \frac{5}{s} - \frac{10}{s+1} + \frac{4}{s+2}$$

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## QUESTION 2

### Method 1

$$Z_1 = R_1 // \frac{1}{sC_1} \quad \text{and} \quad Z_2 = \frac{1}{sC_2} + R_2$$

$$Z_1 = \frac{R_1}{1 + sR_1C_1} \quad \text{and} \quad Z_2 = \frac{1 + sR_2C_2}{sC_2}$$

$$\frac{V_0(s)}{V_i(s)} = \frac{Z_2(s)}{Z_1(s) + Z_2(s)} = \frac{\frac{1 + sR_2C_2}{sC_2}}{\frac{R_1}{1 + sR_1C_1} + \frac{1 + sR_2C_2}{sC_2}} = \frac{\frac{1 + sR_2C_2}{sC_2}}{\frac{sR_1C_2 + (1 + sR_1C_1)(1 + sR_2C_2)}{(1 + sR_1C_1)sC_2}}$$

$$\therefore \frac{V_0(s)}{V_i(s)} = \frac{(1 + sR_1C_1)(1 + sR_2C_2)}{sR_1C_2 + (1 + sR_1C_1)(1 + sR_2C_2)}$$

### Method 2

Equating currents at the output node  $a$  yields

$$\frac{1}{R_1}(v_i - v_0) + C_1 \frac{d}{dt}(v_i - v_0) = i$$

The voltage  $v_0$  and the current  $i$  are related by

$$\frac{1}{C_2} \int_0^t i dt + iR_2 = v_0$$

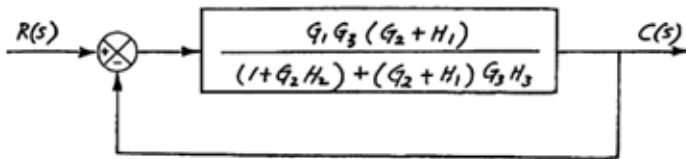
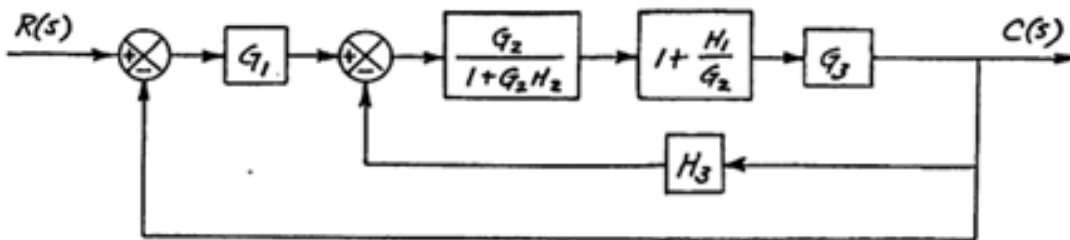
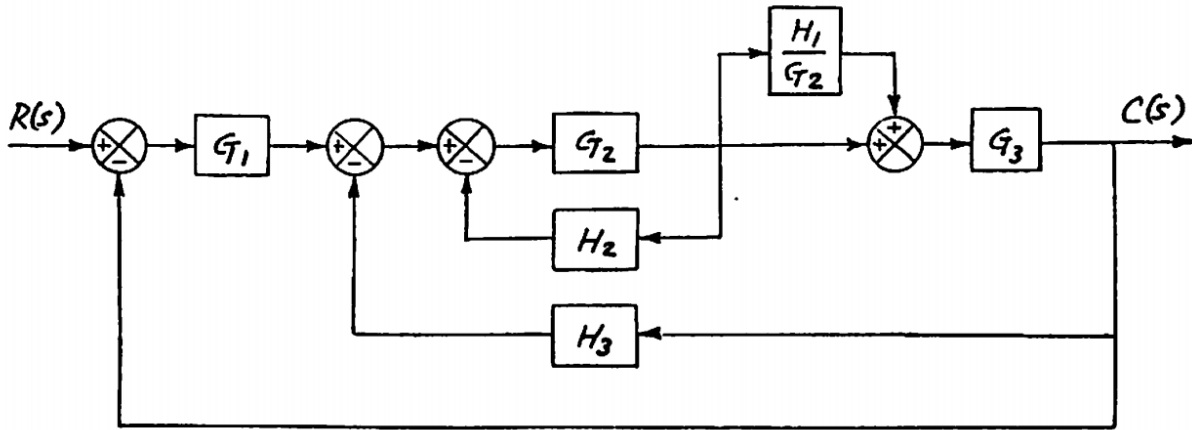
Taking the Laplace Transform of these 2 equations (with zero initial conditions) and eliminating  $I(s)$  results in the equation

$$\left(\frac{1}{R_1} + C_1s\right)[V_i(s) - V_0(s)] = \frac{V_0(s)}{1/sC_2 + R_2}$$

The transfer function of the network is therefore,

$$\therefore \frac{V_0(s)}{V_i(s)} = \frac{\left(s + \frac{1}{R_1C_1}\right)\left(s + \frac{1}{R_2C_2}\right)}{s^2 + \left(\frac{1}{R_1C_1} + \frac{1}{R_2C_2} + \frac{1}{R_2C_1}\right)s + \frac{1}{R_1C_1R_2C_2}}$$

**QUESTION 3**



$$\frac{C(s)}{R(s)} = \frac{G_1 G_2 G_3 + G_1 G_3 H_1}{1 + G_2 H_2 + G_2 G_3 H_3 + G_3 H_1 H_3 + G_1 G_2 G_3 + G_1 G_3 H_1}$$

**QUESTION 4**

(a)  $X_1$

(b)  $X_8$

(c)

ABCDE

HCDE

N

(d)

AI

DL

HJI

NGKJI

BJ

EM

DEG

CK

F

NMLKJI