

## SEHS4653 Control System Analysis Tutorial Questions (Part 3)

### Bode Plot

1. Plot the asymptotic and exact Bode diagrams of the open-loop transfer function,

$$G(s) = \frac{10(s + 1)}{(s + 2)(s + 5)}.$$

2. Draw the exact Bode diagram for the following open-loop transfer function using a frequency range from 0.05 to 0.25 rad/s, in step of 0.05 rad/s.

$$G(s) = \frac{2}{(1 + 2s)(1 + 3s)(1 + 11s)^2}$$

### Gain and Phase Margin

3. Determine the value of  $K$  for the open-loop transfer function of a control system,

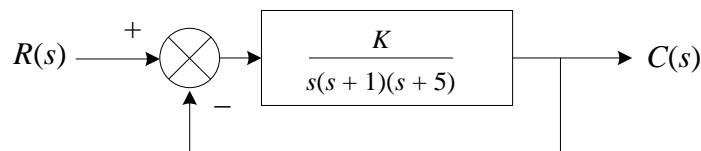
$$G(s) = \frac{K}{s(s + 2)(s + 10)}$$

such that the system may have

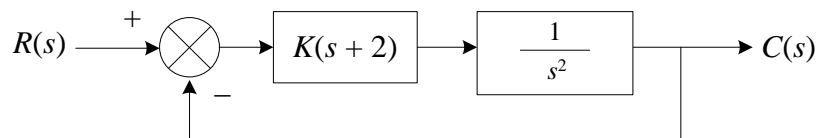
- (a) a gain margin of 6 dB; and (b) a phase margin of  $45^\circ$  **analytically**.  
 (c) Repeat (a) and (b) **graphically** by using  $\omega = 0.01, 0.04, 0.08, 0.1, 0.5, 0.8, 1, 5, 8, 10$  and  $20$  rad/s.

(Ans: (a)  $K = 120.28$ ; (b)  $K = 37.22$ ; (c) 157.18 and 35.18)

4. Obtain the phase and gain margins of the system shown below for the two cases: (a)  $K = 10$  and (b)  $K = 100$  by plotting Bode Diagram. Which system is stable? (Ans: (a) Gain margin = 8.3 dB, phase margin =  $26^\circ$ ; (b) Gain margin = -11 dB, phase margin =  $-19^\circ$ )



5. Below shows a block diagram of a space vehicle control system. Determine the gain  $K$  such that the phase margin is  $50^\circ$ . (Ans:  $K = 1.826$ )



End of Tutorial Questions (Part 3)