Tutorial Bode Plot

Question 1

Construct the asymptotic Bode plots for the frequency response function

$$GH(j_{\omega}) = \frac{1 + j_{\omega}/2 - (\omega/2)^2}{j_{\omega}(1 + j_{\omega}/0.5)(1 + j_{\omega}/4)}$$

Question 2

Construct Bode plots for the frequency response function
$$GH(j_{\omega}) = \frac{2}{j_{\omega}(1+j_{\omega}/2)(1+j_{\omega}/5)}$$

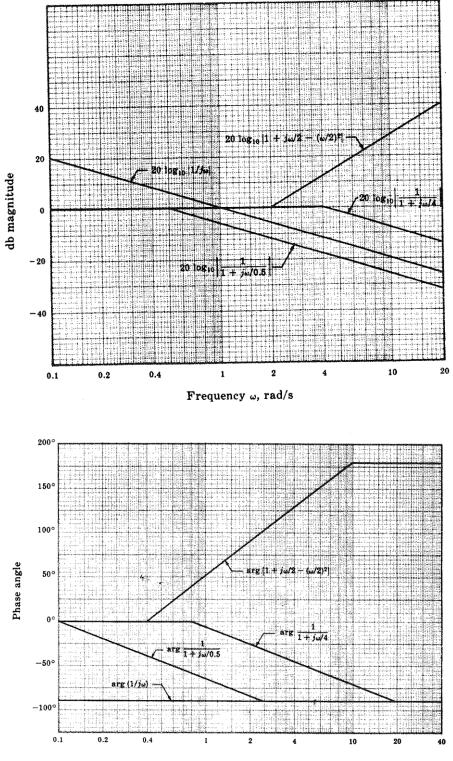
Question 3

**EXAMPLE 8-1** Draw the Bode diagram for the following transfer function:

$$G(j\omega) = \frac{10(j\omega + 3)}{(j\omega)(j\omega + 2)[(j\omega)^2 + j\omega + 2]}$$

## Solution

Question 1



Frequency  $\omega$ , rad/s

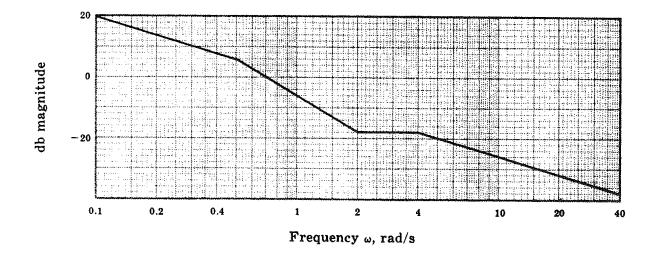
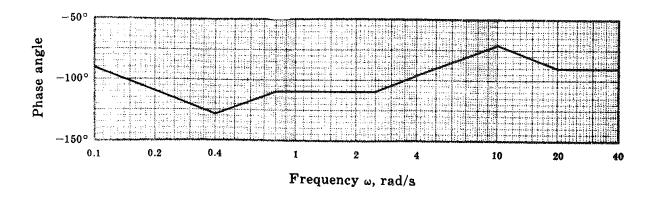


Fig. 15-21



## Question 2

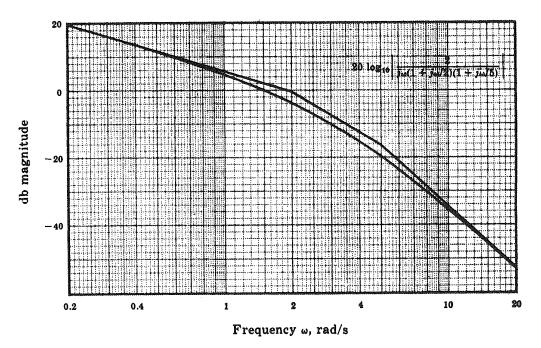
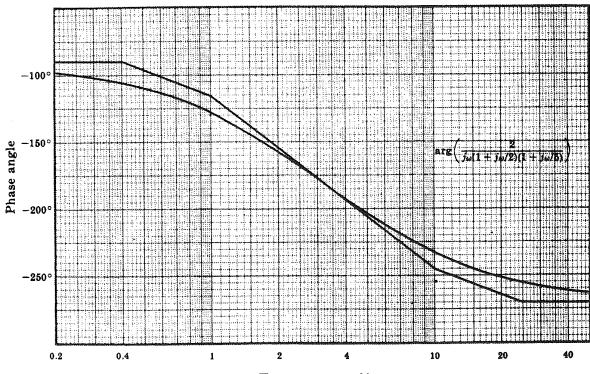


Fig. 15-23

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Frequency  $\omega$ , rad/s

**Question 3** 

Draw the Bode diagram for the following transfer function:

$$G(j\omega) = \frac{10(j\omega + 3)}{(j\omega)(j\omega + 2)[(j\omega)^2 + j\omega + 2]}$$

Make corrections so that the log-magnitude curve is accurate.

To avoid any possible mistakes in drawing the log-magnitude curve, it is desirable to put  $G(j\omega)$  in the following normalized form, where the low-frequency asymptotes for the first-order factors and the second-order factor are the 0-dB line.

$$G(j\omega) = \frac{7.5\left(\frac{j\omega}{3} + 1\right)}{(j\omega)\left(\frac{j\omega}{2} + 1\right)\left[\frac{(j\omega)^2}{2} + \frac{j\omega}{2} + 1\right]}$$

This function is composed of the following factors:

7.5, 
$$(j\omega)^{-1}$$
,  $1+j\frac{\omega}{3}$ ,  $\left(1+j\frac{\omega}{2}\right)^{-1}$ ,  $\left[1+j\frac{\omega}{2}+\frac{(j\omega)^2}{2}\right]^{-1}$ 

The corner frequencies of the third, fourth, and fifth terms are  $\omega = 3$ ,  $\omega = 2$ , and  $\omega = \sqrt{2}$ , respectively. Note that the last term has the damping ratio of 0.3536.

